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Theorem. Consider $\triangle A B C$ and six points $A_{1}, A_{1}^{\prime} \in B C, B_{1}, B_{1}^{\prime} \in C A$, $C_{1}, C_{1}^{\prime} \in A B$ that do not coincide with $A, B, C$. Let $A_{2}$ be the point, other than $A$, that circles $\left(A A_{1} A_{1}^{\prime}\right)$ and $(A B C)$ intersect and define $B_{2}, C_{2}$ cyclically. Let $A_{3}=B B_{2} \cap C C_{2}, B_{3}=C C_{2} \cap A A_{2}, C_{3}=A A_{2} \cap B B_{2}$.

Then $\triangle A_{3} B_{3} C_{3}$ and $\triangle A B C$ are perspective if and only if six points $A_{1}, A_{1}^{\prime}$, $B_{1}, B_{1}^{\prime}, C_{1}, C_{1}^{\prime}$ lie on the same conic.


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